

1-4 Homework

Match statements 1–8 with the property, a – h, that the statement illustrates.

a. Commutative Property of Addition:	$a + b = b + a$
b. Commutative Property of Multiplication:	$a \cdot b = b \cdot a$
c. Additive Identity:	$a + 0 = a$
d. Multiplicative Identity:	$a \cdot 1 = a$
e. Associative Property of Addition:	$(a + b) + c = a + (b + c)$
f. Associative Property of Multiplication:	$(a \cdot b) \cdot c = a \cdot (b \cdot c)$
g. Zero Property of Multiplication:	$a \cdot 0 = 0$
h. Multiplicative Property of -1:	$-1 \cdot a = -a$

1. $12 + 917 = 917 + 12$

2. $5 \cdot 0 = 0$

3. $35 \cdot x = x \cdot 35$

4. $(x \cdot 3) \cdot 4 = x \cdot (3 \cdot 4)$

5. $m + 0 = m$

6. $25 \cdot 1 = 25$

7. $(15 + 9) + 11 = 15 + (9 + 11)$

8. $-1 \cdot 6 = -6$

Simplify each expression. Justify each step that has not been justified.

$$\begin{aligned} 9. \quad 5 + (3x + 2) &= 5 + (2 + 3x) \\ &= (5 + 2) + 3x \\ &= 7 + 3x \end{aligned}$$

Commutative Property of Addition

Combine like terms.

$$\begin{aligned} 10. \quad 3 \cdot (x \cdot 6) &= 3 \cdot (6 \cdot x) \\ &= (3 \cdot 6) \cdot x \\ &= 18x \end{aligned}$$

Associative Property of Multiplication

Multiply.

1-4 Homework (continued)

Simplify each expression. Justify each step.

11. $(2 + 7m) + 5$

12. $9 \cdot (r \cdot 21)$

Tell whether the expressions in each pair are equivalent.

13. $2x$ and $2x \cdot 1$

14. $(5 - 2) \cdot x$ and $3x$

15. $8 + 6 + b$ and $8 + 6b$

16. $5 \cdot (4 - 4)$ and 0

17. You have prepared 40 mL of vanilla, 20 mL of chocolate, and 50 mL of milk for a milkshake.

- How many milliliters of milkshake will you have if you first pour the vanilla, then the chocolate, and finally the milk into your glass?
- How many milliliters of milkshake will you have if you first pour the chocolate, then the vanilla, and finally the milk into your glass?
- Explain how you can tell whether the amounts of milkshake described in parts (a) and (b) are equal.

Use deductive reasoning to tell whether each statement is *true* or *false*. If it is false, give a counterexample.

18. For all real numbers a and b , $a - b = b - a$.

19. For all real numbers p , q , and r , $p - q - r = p - r - q$.

20. For all real numbers x , y , and z , $(x + y) + z = z + (x + y)$.

21. For all real numbers n , $n + 1 = n$.

22. **Writing** Explain why the commutative and associative properties do not hold true for subtraction and division.